Rotational bands and signature inversion phenomena in $\pi h_{9/2} \otimes \nu i_{13/2}$ and $\pi i_{13/2} \otimes \nu i_{13/2}$ structures in odd-odd ¹⁷⁶Ir

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Abstract. High-spin states in ¹⁷⁶Ir have been investigated via the ¹⁴⁹Sm(³¹P,4n γ)¹⁷⁶Ir reaction through excitation functions, X- γ and γ - γ coincidence measurements. Four rotational bands have been identified for the first time and their configurations are suggested on the basis of the existing knowledge of band structures in odd-odd nuclei as well as the measured in-band B(M1)/B(E2) ratios. Among the four bands observed, the $\pi h_{9/2} \otimes \nu i_{13/2}$ and $\pi i_{13/2} \otimes \nu i_{13/2}$ bands exhibit an anomalous signature splitting. The signature inversion point is observed in the former at $I_c = 18\hbar$ which is consistent with expectations; this signature inversion spin in the $\pi i_{13/2} \otimes \nu i_{13/2}$ band may be larger than 25 \hbar . The combined effects of Coriolis and p-n residual interactions involved in such an inversion phenomenon have been discussed qualitatively.

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Signature inversion [1] is a very interesting phenomenon observed in a number of deformed odd-odd nuclei (see ref. [2] and references therein) and it has been attracting large experimental [3] and theoretical [4] interests. Up to date, the signature inversion has been systematically observed throughout the chart of nuclides in the $\pi g_{9/2} \otimes \nu g_{9/2}$, $\pi h_{11/2} \otimes \nu h_{11/2}$, $\pi h_{11/2} \otimes \nu i_{13/2}$ and $\pi h_{9/2} \otimes \nu i_{13/2}$ configurations. Systematic analyses for the first three configurations have been done by Bermúdez and Cardona [5]. Analysis for the $\pi h_{9/2} \otimes \nu i_{13/2}$ structure shows that the critical spin I_c , at which the two $\Delta I = 2$ signature branches cross with each other, seems to decrease (increase) $2-3\hbar$ while decreasing two neutrons (protons) for a chain of isotopes (isotones) [6]. If this regularity could be extended to a wide range of nuclei, one may expect to observe such an inversion spin around $I_{\rm c}\,\sim\,18\hbar$ in ¹⁷⁶Ir. On the other hand, such signature inversion bands systematically investigated correspond to the highj spherical parentage, it is thus a natural assumption that the $\pi i_{13/2} \otimes \nu i_{13/2}$ bands of high-*j* parentage may present a similar inversion phenomenon; the $\pi i_{13/2}(\frac{1}{2}^+[660])$ orbital is involved instead of the $\pi h_{9/2}(\frac{1}{2}[541])$ in the $\pi h_{9/2} \otimes \nu i_{13/2}$ structure [7]. With these points in mind, great efforts have been devoted recently to the studies of in-beam $\gamma\text{-ray}$ spectroscopy in odd-odd $^{176,178}\mathrm{Ir}$ and $^{182}\mathrm{Au}.$ We concentrated on the observation of critical spin $I_{\rm c}$ in the $\pi h_{9/2} \otimes \nu i_{13/2}$ band; this could be regarded as an indirect evidence of signature inversion in spite of the uncertainties in spin assignment. Meanwhile, much attention has been paid to establish the interband transitions from the expected $\pi i_{13/2} \otimes \nu i_{13/2}$ structure to a low-lying 2-quasiparticle band. We have noticed the fact that the $\nu i_{13/2}$ bands are yrast in the neighboring odd-N nuclei, and the excitation energy of the $\pi i_{13/2}$ band member $\frac{13}{2}^+$ decreases from 0.807 MeV in $^{177}\mathrm{Ir}$ to 0.66 MeV in $^{175}\mathrm{Ir}$ [8]. Thus, the $\pi i_{13/2} \otimes \nu i_{13/2}$ band in ¹⁷⁶Ir may locate at lower excitations with respect to the same band in ¹⁷⁸Ir, making it easier to observe the $\pi i_{13/2} \otimes \nu i_{13/2}$ band in 176 Ir. Prior to this work, no high-spin data on $^{176}\mathrm{Ir}$ were available in the literature [9]. Bosch et al. proposed [10] the spin and parity of 5^+ for the ground state of 176 Ir according to the intense β^+/EC feeding to the 6⁺ rotational state in ¹⁷⁶Os. Preliminary results of this research subject have been reported in refs. [6, 11, 12]. During the course

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Fig. 1. Partial level scheme of 176 Ir deduced from the present work.

of this investigation, Hojman *et al.* reported the observation of signature inversion in the $\pi i_{13/2} \otimes \nu i_{13/2}$ band in ¹⁷⁸Ir [13].

The experiment was performed at the Japan Atomic Energy Research Institute (JAERI). The 149 Sm(31 P, $4n\gamma$) 176 Ir reaction was induced by a 31 P beam provided by the JAERI tandem accelerator. The target was an enriched $^{149}\mathrm{Sm}$ metallic powder of 2.1 mg/cm² thickness evaporated on to a 5.5 mg/cm² Pb backing layer. A γ -ray detector array [14] was used comprising 11 HPGe's and one LOAX with BGO anti-Compton shields. The detectors were calibrated with ⁶⁰Co, ¹³³Ba, and ¹⁵²Eu standard sources; typical energy resolution was about 2.0–2.5 keV at FWHM for the 1332.5 keV line. In order to identify the in-beam γ -rays belonging to ¹⁷⁶Ir, we measured an excitation function by varying the ³¹P beam from 145 MeV to 160 MeV with 5 MeV energy steps. The γ spectrum in this experiment was very complex; the photon peaks were often doublets or contaminated by the γ -rays from other reaction channels, and therefore we used coincidence mode in the excitation function measurements. At each beam energy, about $5-10 \times 10^6 \gamma \gamma$ coincidence events were accumulated and sorted on-line into a $4k \times 4k$ matrix. The Ir K X-ray gated γ -ray spectra were projected and analyzed with cares during the experiment; the intensities of known

 γ -rays from ¹⁷⁷Ir/¹⁷⁵Ir decrease/increase apparently with increasing the beam energy, whereas numerous unknown γ -rays were found to have comparable intensities as those from ¹⁷⁷Ir and ¹⁷⁵Ir at beam energies of 145 MeV through 155 MeV. These unknown γ -rays were considered to be emanated most probably from ¹⁷⁶Ir, and finally a beam energy of 155 MeV was used for γ - γ coincidence measurements. About 350 million coincidence events were accumulated and sorted into $4k \times 4k$ matrices for off-line analysis. The relatively intense γ -rays were from the fusion-evaporation residues of 175,176,177 Ir, 175,176 Os, and 173 Re corresponding to 5n, 4n, 3n, 4np, 3np, and $\alpha 3n$ evaporation channels, respectively. Fortunately, the detailed high-spin level schemes for 175,177 Ir, 175,176 Os and 173 Re are available. These known information on 175,177 Ir, 175,176 Os and 173 Re, and the measurements of excitation functions and Ir K X- γ coincidences helped us assign new rotational bands in $^{'176}$ Ir.

The partial level scheme of 176 Ir deduced from the present work is shown in fig. 1. A selected single-gate coincidence spectrum and a sum-gate spectrum are displayed in fig. 2, showing the quality of the data. The γ -transition energies in the level scheme are within an uncertainty of 0.5 keV, and the ordering of the transitions within the bands is established on the basis of γ - γ coin-



Fig. 2. Selected coincidence spectra for bands 3 and 4. The interband transitions (254, 379, and 482.3 keV lines) can be seen clearly in the upper panel of the figure.

Channel

cidence relationships, γ -ray energy sums and γ -ray relative intensities. No linking transitions have been observed from band 1 to bands 2, 3, and 4. The 97.8 keV line deexcites the (8^{-}) band head of band 2, and its DCO ratio is measured to be 0.66(10) corresponding to a stretched $\Delta I = 1$ dipole transition (the DCO ratios are close to unity for the stretched $\Delta I = 2$ quadrupole transitions for the detector array used here). The total internal conversion coefficient for the 97.8 keV transition was extracted to be $\alpha_{\rm T} = 0.80(15)$ based on the argument of intensity balance between the 121 keV and 97.8 keV lines in the 141 keV gated spectrum (theoretical value of $\alpha_{\rm T}$ (121 keV; M1 = 3.684 was used in the calculation). This experimental conversion coefficient is close to the theoretical one of $\alpha_{\rm T}(97.8 \text{ keV}; E1) = 0.43$, thus, we tentatively placed the 97.8 keV γ -ray to feed to the (7⁺) level of band 3; no other interband transition between band 2 and band 3 could be identified. Band 3 and band 4 are connected through several interband transitions (one can see clearly the 254, 379, and 482.3 keV lines in the upper panel of fig. 2). The connection between the two bands has been established as shown in fig. 1, which fix unambiguously the spin and parity of one band relative to the other and thus facilitates their configuration assignments.

According to the classification of coupling scheme for odd-odd nuclei proposed by Kreiner $et \ al. \ [15]$, and

considering the fact that the $\pi 1/2^{-541}$, $\pi 9/2^{-514}$ and $\pi 1/2^+$ [660] bands in ¹⁷⁵Ir [8] and the $\nu 1/2^-$ [521], $\nu 5/2^{-}[512]$ and $\nu 7/2^{+}[633]$ bands in ¹⁷⁵Os [16] are strongly populated in the heavy-ion-induced fusionevaporation reactions, we propose the configurations of $\pi h_{9/2}(1/2^{-}[541]) \otimes \nu i_{13/2}(7/2^{+}[633]), \pi h_{11/2}(9/2^{-}[514]) \otimes$ $\nu i_{13/2}(7/2^+[633]), \ \pi h_{11/2}(9/2^-[514]) \otimes \nu 5/2^-[512], \ {\rm and}$ $\pi i_{13/2}(1/2^+[660]) \otimes \nu i_{13/2}(7/2^+[633])$ for bands 1, 2, 3, and 4, respectively. Indeed, the $\pi h_{9/2} \otimes \nu i_{13/2}$ and $\pi h_{11/2} \otimes$ $\nu i_{13/2}$ bands have been identified in many odd-odd nuclei in this region, and they exhibit very similar level spacings and decay patterns (e.g., in 176 Re [3] and 178 Ir [6]). Therefore the band head spins and parities are proposed to be $I_0^{\pi} = (8^-)$ for band 1 and $I_0^{\pi} = \Omega_{\rm p} + \Omega_{\rm n} = (8^-)$ for band 2 which are consistent with systematics. Band 3 have an effective $K_{\text{eff}} = (2-X)/(X-1) = 7.2$ (X is the energy ratio of first two in-band $\varDelta I=1$ transitions) close to the projection quantum number $K = \Omega_{\rm p} + \Omega_{\rm n} = 9/2 + 5/2 = 7.$ This high value corresponds to a case in which both proton and neutron orbitals are weakly affected by the Coriolis interaction, resulting in $K_{\text{eff}} \approx K = \Omega_{\text{p}} + \Omega_{\text{n}} = 7$ [17]. Consequently, the spin and parity for the lowest level of band 3 have been assigned to be $I_0^{\pi} = K^{\pi} = 7^+$. It should be noted that the $\pi h_{11/2} \otimes \nu 5/2^{-512}$ band has been identified in 178 Ir [11,13] which shows similar level spacings as band 3 in 176 Ir. Based on the spin and parity assignments



Fig. 3. Plot of quasiparticle alignments $i_x vs. \hbar \omega$. The common Harris parameters $(J_0 = 21 \text{ MeV}^{-1}\hbar^2, J_1 = 110 \text{ MeV}^{-3}\hbar^4)$ are used for all the bands. Band 2, showing similar pattern as band 3, is not presented in this figure.



Fig. 4. Experimental B(M1)/B(E2) ratios for bands 3 and 4 together with the geometric model calculations [3] under the assumptions of proposed configurations indicated on the panel. Common parameters $g_R = Z/A = 0.438$ and $Q_0 = 7.0$ eb are used. Other parameters $(i_n, g_{\Omega_n}, \langle K_n \rangle, i_p, g_{\Omega_p}, \langle K_p \rangle, \langle K_{p-n} \rangle)$ are used as (1.0, -0.31, 5/2, 1.0, 1.29, 9/2, 7) for the $\pi h_{11/2} \otimes \nu 5/2^{-}$ [512] configuration, and (4.0, -0.25, 7/2, 6.0, 1.124, 1/2, 3.5) for the $\pi i_{13/2} \otimes \nu i_{13/2}$ configuration, respectively.

for band 3 and the observed linking transitions between band 3 and band 4, the spin and parity for band 4 can be fixed as shown in fig. 1.

Figure 3 presents a plot of quasiparticle alignments i_x versus rotational frequency $\hbar\omega$. In this plot, a common reference ($J_0 = 21 \text{ MeV}^{-1} \hbar^2, J_1 = 110 \text{ MeV}^{-3} \hbar^4$) has been used in order that the alignment for band 1 is roughly constant. As is clear from this figure, large alignment for band 4 strongly suggests that the high-j orbitals both for proton and neutron have been involved. The alignment in the $\pi h_{9/2} \otimes \nu i_{13/2}$ band is roughly $i_x(\omega) \sim 7.5\hbar$, only the $\pi i_{13/2} \otimes \nu i_{13/2}$ two-quasiparticle band can have such alignment as high as $\sim 10\hbar$; the $i_{13/2}$ proton contributes more



Fig. 5. Plot of signature splittings S(I) vs. I for the $\pi h_{9/2} \otimes \nu i_{13/2}$ (upper panel) and $\pi_{13/2} \otimes \nu i_{13/2}$ (lower panel) bands in both ¹⁷⁶Ir (present work) and ¹⁷⁸Ir [11,13]. The arrows indicate the inversion spin.

than $6\hbar$ [8], whilst the rest originates from the $i_{13/2}$ neutron [16]. In fact, this band has been identified in ¹⁷⁸Ir [11, 13] and ¹⁸²Au [12] which show a structure very similar to band 4 in ¹⁷⁶Ir. Figure 4 presents the experimental B(M1)/B(E2) ratios for bands 3 and 4 together with the geometrical model calculations [3]. It is clear from this figure that the experimental B(M1)/B(E2) ratios can be well reproduced under the assumption of the proposed configurations.

According to the configuration and spin-parity assignments, it is now interesting to point out that the signature splitting in the $\pi h_{9/2} \otimes \nu i_{13/2}$ and $\pi i_{13/2} \otimes \nu i_{13/2}$ bands of odd-odd $^{176}\mathrm{Ir}$ is inverted at low and medium spins. To illustrate further the features of signature inversion, we compare the typical staggering curves S(I) = $E(I) - E(I-1) - \frac{1}{2}[E(I+1) - E(I) + E(I-1) - E(I-2)]$ vs. I in fig. 5 for the $\pi h_{9/2} \otimes \nu i_{13/2}$ and $\pi i_{13/2} \otimes \nu i_{13/2}$ bands in both ¹⁷⁶Ir and ¹⁷⁸Ir. The similar staggering pattern is impressive, *i.e.*, the $\alpha_{\rm f}^{\rm p-n} = \alpha_{\rm f}^{\rm p} + \alpha_{\rm f}^{\rm n} = \frac{1}{2} + \frac{1}{2} = 1$ favored signature branch (odd-spin sequence) lies higher than the $\alpha_{uf}^{p-n} = \alpha_f^p + \alpha_{uf}^n = \frac{1}{2} - \frac{1}{2} = 0$ unfavored signature branch (even-spin sequence); this is the so-called low-spin signature inversion [1]. On the other hand, the signature splitting reverts to the normal ordering at $I_c = (18^-)$ for the $\pi h_{9/2} \otimes \nu i_{13/2}$ band in ¹⁷⁶Ir. This critical spin is $3\hbar$ lower than that in ¹⁷⁸Ir which is consistent with systematic expectations [6]. For the $\pi i_{13/2} \otimes \nu i_{13/2}$ band in ¹⁷⁶Ir, the critical inversion spin has not been reached in this work, indicating that the critical inversion spin I_c should be larger than $25\hbar$.

The low-spin signature inversion in the $\pi h_{9/2} \otimes \nu i_{13/2}$ bands has been discussed in the framework of 2quasiparticle plus rotor model in several recent publicaltions (*e.g.*, refs. [3,7] and references therein); it has been demonstrated that the particle-hole component of protonneutron residual interaction plays a key role for the lowspin signature inversion. The inversion phenomena in the

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 $\pi i_{13/2} \otimes \nu i_{13/2}$ bands may be understood, as proposed by Hojman et al. [13], in the same theoretical framework of the Particle Rotor Model with p-n interaction. In fact, the signature splitting (or level staggering) in both bands is determined by two important factors, *i.e.*, the Coriolis and p-n residual interactions. The Coriolis force favors a normal signature splitting, namely, the odd-spin sequence is lower in energy than the even-spin levels, whereas the inclusion of p-n residual interaction will lead to an inverted signature splitting; this has been studied many years ago by Kreiner in the case of oblate odd-odd Tl isotopes [18]. The competition between the Coriolis and p-n residual interactions results in the level staggering pattern as shown in fig. 5; the signature splitting is inverted at low and medium spins (signature inversion) when the p-n residual interaction dominates, and the normal signature splitting is restored at higher spins when Coriolis interaction dominates. Thus the critical inversion spin $I_{\rm c}$ should be related to the combined effects of Coriolis and p-n residual interactions. The inversion spins in the $\pi i_{13/2} \otimes \nu i_{13/2}$ bands are observed to be larger than that in the $\pi h_{9/2} \otimes \nu i_{13/2}$ bands as clearly demonstrated in fig. 5; this may be understood, at least qualitatively, by considering the two points: 1) Both quasi-proton and quasi-neutron occupy the same high-j orbitals in the $\pi i_{13/2} \otimes \nu i_{13/2}$ structures, thus the residual p-n interaction could be stronger than that in the $\pi h_{9/2} \otimes \nu i_{13/2}$ bands. The strong residual p-n interaction tends to keep the inverted signature splitting up to high spins. 2) The $\pi i_{13/2}(\frac{1}{2}^+[660])$ proton drives the nucleus towards a larger quadrupole deformation, this will reduce the amplitute of normal signature splitting caused by the Coriolis force. As a result, the restoration to the normal signature splitting in the $\pi i_{13/2} \otimes \nu i_{13/2}$ bands is retarded with respect to the case in the $\pi h_{9/2} \otimes \nu i_{13/2}$ bands. The inversion spin $I_{\rm c}$ for the $\pi h_{9/2} {\otimes} \nu i_{13/2}$ band in $^{176}{\rm Ir}$ is $3\hbar$ lower than that in the same band of 178 Ir; this could be interpreted probably due to the lowering of the neutron Fermi surface and the reduced deformation of the core [19]; both will enhance the normal signature splitting caused by the Coriolis interaction and lead to an early restoration to the normal signature splitting. We are not able to understand the non-observation of such inversion spin in the $\pi i_{13/2} \otimes \nu i_{13/2}$ band of ¹⁷⁶Ir up to $I^{\pi} = (25^+)\hbar$, this is certainly in need of further investigations.

In conclusion, an in-beam γ -spectroscopy experiment has been performed leading to the observation of four rotational bands in odd-odd ¹⁷⁶Ir. The quasiparticle configurations and the level spin assignments for each band have been proposed on the basis of several considerations, *i.e.*, quasiparticle alignments, signature splitting, in-band B(M1)/B(E2) ratios, and level spacing systematics, as well as the knowledge in neighboring nuclei. The interband connection from the $\pi i_{13/2} \otimes \nu i_{13/2}$ structure to the proposed $\pi h_{11/2} \otimes \nu \frac{5}{2}^{-1}$ [512] band has been established leading

to the signature inversion for the $\pi i_{13/2} \otimes \nu i_{13/2}$ band at low and medium spins. The signature inversion in the $\pi h_{9/2} \otimes \nu i_{13/2}$ band has been confirmed by the observation of signature crossing at $I \sim 18\hbar$ which is consistent with systematic expectations. The patterns of signature splitting in the two bands of both ¹⁷⁶Ir and ¹⁷⁸Ir are discussed, qualitatively, on the basis of the combined effects of Coriolis and p-n residual interactions. A deeper understanding on the inversion phenomena in both the $\pi h_{9/2} \otimes \nu i_{13/2}$ and the $\pi i_{13/2} \otimes \nu i_{13/2}$ structures, and on the different features presented in ¹⁷⁶Ir and ¹⁷⁸Ir is in need of further investigations; this is however beyond the scope of this paper. We would like to emphasize that the observation of such inversion phenomena in both 176 Ir and 178 Ir provides an interesting test ground for different theoretical interpretations.

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References

- 1. R. Bengtsson et al., Nucl. Phys. A 415, 189 (1984).
- L.L. Riedinger *et al.*, Prog. Part. Nucl. Phys. **38**, 251 (1997).
- 3. M.A. Cardona et al., Phys. Rev. C 59, 1298 (1999).
- F.R. Xu *et al.*, Nucl. Phys. A 669, 119 (2000) and references therein.
- G. García Bermúdez, M.A. Cardona, Phys. Rev. C 64, 034311 (2001).
- 6. Y.H. Zhang et al., Eur. Phys. J. A 8, 439 (2000).
- 7. R.A. Bark *et al.*, Phys. Lett. B **406**, 193 (1997).
- 8. G.D. Dracoulis et al., Nucl. Phys. A 534, 173 (1991).
- 9. E. Browne, J. Huo, Nucl. Data Sheets 84, 337 (1998).
- 10. U. Bosch et al., Z. Phys. A 336, 359 (1990).
- 11. Y.H. Zhang et al., Chin. Phys. Lett. 18, 1323 (2001).
- Y.H. Zhang et al., Proceedings of the 8th National Conference on Nuclear Structure, 24-31 March 2000 Hakou, China; High Energy Phys. & Nucl. Phys. 24, Suppl. 21 (2000) (in Chinese).
- 13. D. Hojman et al., Eur. Phys. J. A 10, 245 (2001).
- K. Furuno *et al.*, Nucl. Instrum. Methods Phys. Res. A 421, 211 (1999).
- 15. A.J. Kreiner et al., Phys. Rev. C 36, 2309 (1987).
- 16. B. Fabricius et al., Nucl. Phys. A 511, 345 (1990).
- 17. D. Hojman et al., Phys. Rev. C 45, 90 (1992).
- 18. A.J. Kreiner, Phys. Rev. C 22, 2570 (1980).
- R. Bengtsson, Proceedings of the International Conference on High Spin Physics and Gamma-Soft Nuclei, Pittsburgh, PA USA, 1990, edited by J.X. Saladin, R.A. Sorensen, C.M. Vincent (World Scientific, Singapore, 1990) p. 289.